

Ex: The spread of a flu in a certain school is modeled by the equation  $P(t) = \frac{100}{1+e^{3-t}}$  where  $P(t)$  is the total number of students infected  $t$  days after the flu was first noticed.

$$100(1+e^{3-t})^{-1}$$

a. Estimate the initial number of students infected.

$$P(0) = \frac{100}{1+e^{3-0}} = \frac{100}{1+e^3} \approx 5 \text{ students}$$

b. How fast is the flu spreading after 3 days?

$$P'(t) = -100(1+e^{3-t})^{-2} (e^{3-t})(-1) = \frac{100e^{3-t}}{(1+e^{3-t})^2} \Bigg|_{t=3} = \frac{100e^{3-3}}{(1+e^{3-3})^2} = \frac{100e^0}{(1+e^0)^2}$$

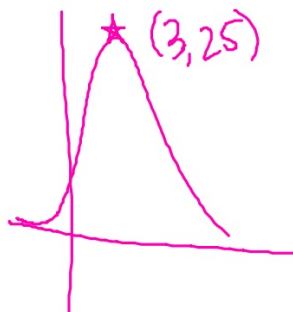
$$= \frac{100}{4} = 25 \text{ Students/day}$$

c. When will the flu spread at its maximum rate? What is this rate?



$$Y_1 = n \text{Deriv}(100/(1+e^{3-t}), X, X)$$

$$(100/(1+e^{3-t}), X, X)$$



The flu will spread at its max rate at approx 3 days and that rate is approx 25 students/day.

p. 179 # 51, 52, 57-62